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Processing and properties of luminescent Cr3+ doped transparent alumina ceramics

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Abstract

Transparent Cr₂O₃-doped alumina ceramics were prepared by slip casting, followed by presintering in ambient atmosphere and hot isostatic pressing. The effect of dopant concentration on material properties, including microstructure and optical properties was evaluated. Real inline transmittance in the range of 20-44 % was measured for the ceramics with the mean grain $size < 520$ nm: the transmittance decreased with increasing grain size and Cr content. The excitation spectra consisted of two broad bands with maxima at 404 nm and 558 nm, corresponding to ${}^4A_{2g} \rightarrow {}^4T_{1g}$ and ${}^4A_{2g} \rightarrow {}^4T_{2g}$ transitions of Cr³⁺ ions in octahedral sites of α -Al2O3. The intensive deep red narrow emissions under violet/green light excitation, R-lines $({}^{2}E_{g} \rightarrow {}^{4}A_{2g}$ transition), were observed at 692.5 nm and 693.8 nm, that are very close to ruby single crystal. The highest emission was achieved at the Cr^{3+} concentration of 0.4 at.%. The

luminescence decay curves exhibited single-exponential behaviour with decay times of \sim 3.6 ms.

Keywords

Alumina; chromium; dopants/doping; luminescence; real in-line transmittance; transparent

ceramics

1. Introduction

A ruby (Cr: Al_2O_3) is not only a gemstone highly valued for centuries, but also the material used in modern technologies such as lasers [1], temperature sensors [2, 3], optoelectronics [4], etc. The exceptional optical, mechanical, thermal and chemical properties of ruby crystals motivate research and development of new materials based on this composition. Numerous studies deal with the preparation of Cr-doped Al_2O_3 powders with different crystal structures, e.g. α and γ [5-7] or Cr-doped alumina microspheres [8]. Some attempts aimed at replacement of single crystals with transparent polycrystalline ceramics were also reported [9-11]. Polycrystalline alumina ceramics offers reduced cost and higher variability of shapes and sizes than single crystals. However, the preparation of transparent polycrystalline alumina is difficult due to birefringence of alumina crystals, and requires precise adjustment of all processing steps. Even after thorough optimisation, the transparency of the polycrystalline alumina ceramics probably cannot reach values typical for ruby crystals.

Vacuum sintering [10] or spark plasma sintering (SPS) [9, 11] were successfully applied for preparation of transparent Cr-doped alumina ceramics. However, only Wang et al. [11] provide accurate information on material's transparency, which is strongly related to the Cr content. The significant decrease of the transparency with increasing dopant amount, especially in the visible region, was recorded.

Present work aims at preparation of transparent Cr^{3+} -doped alumina with various Cr contents, using a processing chain optimised in our previous work on rare-earth doped aluminas [12-15]. This approach includes slip-casting of colloidal suspensions, pressureless pre-sintering followed by hot isostatic pressing (HIP) and ensures careful homogenisation of initial powders, optimal particles´ arrangement in a green body and eliminates carbon contamination during sintering. Attention is paid to attaining fine grained microstructure with homogenous dopants' distribution. In contrast to rare earth elements doped alumina, where the dopants were

distributed along the grain boundaries due to their low solubility in alumina matrix, dissolution of Cr^{3+} in the alumina matrix is expected [16]. Prepared ceramics are thoroughly characterised in terms of their physical, microstructural and optical properties.

The novelty of the present work lies in the evaluation of the effect of Cr^{3+} content on all studied properties and mainly in tailoring of the optimum dopant concentration for the highest photoluminescent intensity and the transparency.

2. Experimental

Chromium doped alumina was prepared from commercial high purity $A₁₂O₃$ powder (purity of 99.99%, TM-DAR, Taimei Chemicals Co., Japan) with the primary particle size of ~150 nm and nano-Cr₂O₃ powder (purity of 99%, GNM – Getnanomaterials, USA) with the primary particle size of $~60$ nm. The content of chromium ranged from 0.10 to 0.75 at.% with respect to Al2O3. The preparation of the samples was carried out according to the procedure described in detail in our recently published papers [12, 13]. The designation of the samples in this work reflects the content of Cr^{3+} ; e.g. Cr0.1 means 0.10 at.% of Cr with respect to alumina.

Dried samples (2 days drying under ambient conditions, then 3 h at 60°C) were pre-sintered in air in order to attain closed porosity. The sintering regime consisted of heating the green bodies to a pre-defined temperature (1350 - 1390°C) at a heating rate of 20 °C min⁻¹, with the dwell time of 2 min. Afterwards the samples were cooled down at the same rate. Pre-sintered samples were HIP-ed at 1200°C for 3 h in argon atmosphere pressurized to 200 MPa.

Density of pre-sintered samples was estimated according to the Archimedes' principle by double weighing method (EN 623-2) in deionised water and related to the theoretical density of alumina (3.99 g cm^{-3}) .

A scanning electron microscope Lyra 3 (Tescan, Czech Republic) with integrated a Time-of-Flight Secondary Ion Mass Spectrometry (TOF-SIMS) analyser was used to examine the microstructure and chemical composition of sintered bodies. The mean grain size (MGS) was estimated by the linear intercept method (EN 623-3) using a correction factor of 1.56 [17]. Minimum of 200 grains were measured to obtain statistically robust set of data.

A non-polarized He–Ne laser with a wavelength of 632.8 nm was utilised for determining the real in-line transmittance (RIT) of polished samples. RIT values were measured in at least ten different positions for each sample and they were recalculated to constant thickness of 0.8 mm.

The UV-VIS-NIR spectra (optical transmission spectra) of the polished samples were measured on a Cary 5000 spectrometer (Agilent, USA) in the spectral range of 200-2500 nm. The samples were placed at normal incidence to the beam path. The spectra were obtained at a scan rate of 300 nm/min. The transmission spectra were corrected for the reflection losses that in the case of alumina corresponds to \sim 14 %, and recalculated to the 0.8 mm sample thickness to compare experimental data with literature reported data.

The photoluminescence excitation and emission spectra were recorded using a Fluorolog FL3- 21 spectrometer (Horiba, Japan) equipped with the photomultiplier tube R928 detector (Hamamatsu Photonics K. K., Japan) operated in photon counting mode. The Xe-lamp (450 W) was used as an excitation light source, and particular excitation wavelength was spectrally filtered using a double monochromator. To eliminate the second-order diffraction of the radiation source on grating, a cut-off filters were used in all measurements. The luminescence spectra of studied samples presented herein were recorded at room temperature in front face mode (backscattering geometry). The luminescence decay curves were recorded at room temperature with the same instrument using a phosphorescence module of the spectrometer. The same flash Xe-lamp was used as an excitation source.

3. Results and discussion

3.1 The effect of Cr3+ on sintering and microstructure of Cr3+ -doped alumina

The preparation of the transparent alumina requires precise adjustment of sintering parameters in order to ensure complete elimination of residual porosity and to inhibit the grain growth. Preliminary experiments with the samples containing 0.1, 0.5 and 0.75 at.% of Cr^{3+} showed that the addition of chromium impaired densification; the effect was more pronounced at higher dopant concentrations (Fig. 1). The temperature required to achieve the state of closed porosity increased slightly with increasing content of Cr^{3+} in the alumina matrix. Based on these preliminary experiments, two pre-sintering temperatures (1380°C and 1390°C) were selected for preparation of samples with closed porosity suitable for HIP. HIP was then performed at 1200°C for 3 h, resulting in transparent ceramics (Fig. 2). The samples were approximately 0.8 mm thick and were placed 10 mm above the background.

Preliminary photoluminescence measurements showed significant concentration quenching for the Cr³⁺ concentration of 0.75 at.%. Therefore, the optical properties of transparent α -Al₂O₃ polycrystalline ceramics are further discussed only for dopant content ranging between 0.1 and 0.5 at.% Cr^{3+} .

The influence of the Cr^{3+} content on the mean grain size of HIP-ed samples is shown in Fig. 3. The MGS of Cr^{3+} -doped alumina ranged from 380 nm to 520 nm: the MGS increased with the increasing pre-sintering temperature. The difference ranged between 50-90 nm for a given Cr^{3+} concentration. At identical conditions of pre-sintering, the MGS decreased gradually with increasing content of chromium. These results indicate that $Cr³⁺$ addition decelerated both densification and grain growth, similarly to e.g. Y^{3+} or Zr^{4+} [18].

The chromium cations have unlimited solubility in an alumina crystal lattice, creating a solid solution in the whole concentration range [16]. However, inclusions or regions enriched by Cr may be formed as the results of insufficient homogeneity or diffusion (due to a short sintering time) that do not allow ideal redistribution of the dopant atoms [12]. To elucidate this effect, harmful for the transparency, a careful examination of the Cr^{3+} distribution in HIP-ed samples was performed. Some typical positive mode TOF-SIMS spectra of $Cr³⁺$ -doped alumina with images of aluminium and chromium distribution are presented in Fig. 4. The TOF-SIMS mass spectra confirmed the presence of Cr^{3+} in the alumina matrix as is documented in detail in the inset figure with the mass range ranging from m/z 49 to m/z 55. A homogeneous distribution of both aluminium and chromium elements is evident from TOF-SIMS images representing projection of the concentration in the z-axis direction (x and y axes belong to the surface region). Nevertheless, from image of chromium distribution it may appear that Cr atoms are in a higher concentration at the surface of sample. This phenomenon was caused by edge effect, when the enhanced excitation of ions from the surface topography occurred. It can be assumed that the processing parameters and thermal treatment allowed fabrication of alumina ceramics with uniform distribution of Cr^{3+} .

3.2 Optical properties of Cr3+ -doped alumina

3.2.1 Real in-line transmittance

The real in-line transmittance is a real indicator of the materials´ transparency [19]. The dependence of the RIT (at a wavelength of 632.8 nm) on Cr^{3+} content is shown in Fig. 5. The RIT ranged from 23% to 44% related to the samples with the thickness recalculated to the same value of 0.8 mm. The transparency was affected both by the MGS and the Cr^{3+} content. The RIT decreased with the increasing content of Cr^{3+} and with the increasing MGS, which is always higher after pre-sintering at 1390°C (see Fig. 3). In the range studied the effect of grain size seems to be more significant than the influence of the Cr^{3+} doping. Generally, the RIT values were relatively low comparing to Eu- or Er-doped aluminas prepared in a similar way [12-15]. This decrease is mainly attributed to the absorption of light by Cr^{3+} ions in the alumina matrix at 632.8 nm (see excitation optical spectra in Fig. 6). This was confirmed also by the luminescence spectra measurements: when the Cr-doped samples were excited at this wavelength (633 nm), relatively low intensity of radiation emitted at 694 nm (Cr^{3+}) was observed with the same spectral profile typical for Cr^{3+} emission (see Fig. 7). Despite of the fact, that absorption at that wavelength is quite low the laser light is sufficient to excite the Cr^{3+} ions and partially convert the 632.8 nm red light into deep-red emission with maximum at 694 nm that is dispersed to all directions.

3.2.2 Optical transmission spectra

The optical transmission spectra of the studied Cr^{3+} -doped transparent alumina with various Cr^{3+} concentrations pre-sintered at 1380°C are shown in Fig. 6a. The transmission spectra exhibit two broad bands with the maxima at 403 nm and 558 nm and one "line" band of low intensity at 694 nm corresponding to absorption of Cr^{3+} ions.

In terms of Tanabe-Sugano energy level diagram that shows the splitting of the Cr^{3+} free ion levels ($d³$ configuration) in an octahedral crystal field as the ratio of crystal field strength to interelectronic repulsion (measured in D_q/B units), five absorption transitions are possible for the ruby with Dq/B value of 2.8 and $B=918$ cm⁻¹; five absorption lines correspond to ${}^{4}A_{2g}({}^{4}F) \rightarrow {}^{4}T_{1g}({}^{4}F),$ ${}^{4}A_{2g}({}^{4}F) \rightarrow {}^{2}T_{2g}({}^{2}G),$ ${}^{4}A_{2g}({}^{4}F) \rightarrow {}^{4}T_{2g}({}^{4}F),$ ${}^{4}A_{2g}({}^{4}F) \rightarrow {}^{2}T_{1g}({}^{2}G),$ ${}^{4}A_{2g}({}^{4}F) \rightarrow {}^{2}E_{g}({}^{2}G)$ electronic transitions [20, 21]. Three dominant bands commonly observed in absorption spectra are violet, green and red centred at \sim 400 nm, 555 nm and 692/694 nm (Rlines). The violet $(^{4}A_{2g}(^{4}F) \rightarrow ^{4}T_{1g}(^{4}F)$ and green $(^{4}A_{2g}(^{4}F) \rightarrow ^{4}T_{2g}(^{4}F)$ transitions as a spinallowed transition result in intensive broad absorption bands; the red ${}^4A_{2g}({}^4F) \rightarrow {}^2E_{2g}({}^2G)$ is spin-forbidden transition of much lower intensity. The weak spin-forbidden quartet-doublet transitions ${}^4A_{2g}({}^4F) \rightarrow {}^2T_{1g}({}^2G)/{}^2T_{1g}({}^2G)$ are rarely observed and resolved in the absorption spectra [20-22].

Compared to the alumina single crystal with almost constant transmission $(\sim 86\%)$ in the whole visible spectral range, the transmission of prepared transparent polycrystalline $Cr³⁺$ -doped alumina samples decreases with decreasing wavelength due to the scattering of the incident light at grain boundaries, which is wavelength dependent. The transmission of prepared samples was found to be similar to the data published previously on the Al_2O_3 : Cr^{3+} doped transparent polycrystalline ceramics [11, 22, 23]. Samples pre-sintered at 1390°C exhibit lower transmission compared to the samples pre-sintered at 1380°C because of larger grain size and larger scattering affect. The transmission spectra were corrected for reflection losses, converted into absorbance scale, normalised to 1 cm thickness, and background corrected using the exponential function to eliminate the light scattering effect at grain boundaries. The absorption spectra are shown in Fig. 6b. The absorbance increased with increasing Cr^{3+} concentration and calculated molar absorption coefficients, ε , (using the linear fit according to the Lambert-Beer law $A/l = \varepsilon c$) for violet and green absorption were found to be $3.8 \pm 0.1 \times 10^4$ mol⁻¹cm² (38 L⁻¹) ¹·mol⁻¹cm) and 2.4 \pm 0.1 \times 10⁴ mol⁻¹cm² (24 L⁻¹·mol⁻¹cm), respectively. Almost identical values were found for samples pre-sintered at 1390° C (36 and 24 L⁻¹·mol⁻¹·cm). The red absorption was too weak to determine the molar absorption coefficient reliably. Absorption cross-section values, σ , for violet and green absorption were calculated to be 1.45 \times 10⁻¹⁹ cm² and 9.22 \times 10⁻¹ 20 cm^2 , respectively. These absorption-cross section (ACS) data corresponds quite well with the average ACS data reported by Dodd et al. [24] for ruby single crystal doped with different concentration of Cr^{3+} ions; 1.98×10^{-19} cm² and 1.20×10^{-19} cm². Somewhat higher ACS data were reported by Cronemeyer [25] for ruby single crystal. The differences between our data and data reported by Dodd et al. [24] and Cronemeyer [25] are most likely due to sample processing, either caused by Cr lost and/or by partial reduction of Cr^{3+} species to Cr^{2+} [26]. Penilla et al. [22] reported a detailed analysis of transmission spectra of polycrystalline Al₂O₃: Cr^{3+} transparent ceramics at Cr^{3+} doping level of 0.5 at.% and 1.0 at.% and grain size

similar to our samples. The applied modified analytical model is based on Rayleigh-Gans-Debye approximation that was already employed for transparent alumina ceramics [19, 27]. The peak absorption coefficients denoted as α (in cm⁻¹) of our sample Cr0.5 were around 16.9 cm⁻¹ (σ = 1.43×10⁻¹⁹ cm²) for violet and 10.4 cm⁻¹ (σ = 8.84×10⁻²⁰ cm²) for green absorption and these values are in a good agreement to those reported by Penilla et al. [22] for the same concentration of Cr^{3+} in Al₂O₃ polycrystalline transparent ceramics (α (violet) = 14.2 cm⁻¹ (σ = 1.20×10⁻¹⁹ cm²) and α (green) = 9.0 cm⁻¹ (σ = 7.63×10⁻²⁰ cm²)). The reported grain size is slightly lower (344 nm) compared to the grain size of our sample (380 nm).

3.2.3 Photoluminescence properties

The excitation (PLE) spectra of HIPed samples pre-sintered at 1380°C are shown in Fig. 7. The PLE spectra monitored at 694 nm show two intensive broad bands centred at 404 nm (24700 cm⁻¹) and 558 nm (17900 cm⁻¹) corresponding to the spin-allowed ${}^4A_{2g}({}^4F) \rightarrow {}^4T_{1g}({}^4F)$ and ${}^4A_{2g}({}^4F) \rightarrow {}^4T_{2g}({}^4F)$ transitions of Cr³⁺ ions in octahedral sites of α -Al₂O₃ [28-30]. The broad nature of these transitions is a consequence of the character of energy states involved in transitions, that are sensitive to distortion of coordination polyhedra, Cr-O bond length and hence, to the ligand field strength around Cr^{3+} ions. The intensity of the violet absorption is higher than the green one, but with increasing Cr^{3+} concentration the intensity of the green absorption increases. For the concentration of 0.5 at.% Cr^{3+} the intensity ratio, $IR =$ $I(^{4}T_{1g})/I(^{4}T_{2g})$, approaches ~1. However in the sample containing 0.75 at.% of Cr³⁺ (spectrum not shown) the value is again reduced to 0.9. The shapes of all spectra are very similar. Similar behaviour was observed also for samples pre-sintered at 1390°C. Analogous effect on PLE intensity ratio was observed by Toyoda et al. [31] for Cr^{3+} -doped Al₂O₃ ceramic and Murphy et al. [32] for polycrystalline ruby samples. The decrease in *IR* value with increasing Cr^{3+} concentration was discussed in details by Murphy using a rate-equation model and is possibly

due to the increase of non-radiative processes at the ² E_g ²G) \rightarrow ⁴ A_{2g} ⁴F) transition, indicating concentration quenching [32]. Two cases observed in PLE spectra of Cr^{3+} -doped Al₂O₃ prepared via different synthetic routes for both lower and higher Cr^{3+} doping levels were reported in the literature: (*i*) The $IR > 1$ with higher absorption intensity in violet-blue spectral range [29, 33, 34] and *(ii)* $IR < 1$ with higher absorption intensity in green-yellow spectral range [28, 30, 35-40], respectively. According to the Tanabe-Sugano diagram for Cr^{3+} (d³ electron configuration), the ${}^{4}T_{1g}$ and ${}^{4}T_{2g}$ energy levels are sensitive to the crystal field strength that is affected by Cr^{3+} ions coordination environment. Thus, distortion of the coordination polyhedra around Cr^{3+} ions, interaction with the host lattice and also defects may affect the dynamics of ${}^{2}E_{g}({}^{2}G) \rightarrow {}^{4}A_{2g}({}^{4}F)$ transition, that is used to monitor light absorption. As a consequence, the method of preparation, sample morphology, and heat treatment may influence the intensity of particular transition in PLE spectra.

The photoluminescence emission (PL) spectra of Cr0.1 under excitation either at 404 nm or 560 nm (see Fig. 8a) exhibited very narrow (with FWHM 23 cm^{-1} and 19 cm^{-1}) so-called zerophonon R-lines (Raman lines R₁ and R₂) at 692.5 nm (14442 cm⁻¹) and 693.8 nm (14412 cm⁻¹) assigned to spin-forbidden ²E_g(²G) \rightarrow ⁴A_{2g}(⁴F) transition originating from isolated Cr³⁺ ions in octahedral sites [28-30, 35, 36, 41] as Cr^{3+} ions substitute Al^{3+} ions in the α -Al₂O₃ lattice. The existence of two R-lines is caused by splitting of the ${}^{2}E_{g}$ excited state that consists of two sublevels, due to spin-orbit coupling. Two observed R-lines, the R_1 and R_2 lines, are separated by 30 cm⁻¹. The R line positions of Cr^{3+} ions in bulk ruby single crystal are 694.3 nm (R₁) and 692.9 nm (R_2) with separation of 29 cm⁻¹ [41, 42]. Thus, the R lines observed in the present work are very close to that of single crystal. The narrow character of the PL emission results from the fact that excited state ${}^{2}E_{g}$ is only slightly influenced by the crystal field strength. The intensity of the PL emission is higher under excitation at 404 nm than at 560 nm for lower Cr^{3+} concentration (see Fig. 8a), however, with increasing concentration the intensities are

comparable and almost identical (for sample containing 0.5 at.% of Cr^{3+}) for both excitation wavelengths, as follows from the PLE spectra (see Fig. 8b). The emissions of the much lower intensity (sidebands) were also observed on the Stokes and anti-Stokes side of R-lines at 658, 669, 675, 680, 707, 713 nm. The weak sharp lines called N-lines observed at 699.3, 701.3, 704.2 nm, indicate the presence of Cr-Cr pairs and can be related to emissions of coupled pairs of Cr^{3+} ions, whereas the sidebands, shorter/longer wavelength broader bands around R lines, are associated to phonon assisted transitions due to the electron-phonon coupling in isolated sites [30, 31, 34, 41, 43, 44]. Moreover, the R_2/R_1 intensity ratio does not show any correlation with Cr content in the range of studied Cr^{3+} concentrations (normalised PL spectra are almost identical) and is 0.67 (for area R_2/R_1 ratios, the value is 0.56). In contrast, the intensity of Nlines increases with increasing Cr content that could be interpreted as a result of growing probability of interactions among neighbouring Cr^{3+} ions.

It is evident that emission intensity strongly depends on doping concentration. The PL intensity increases with increasing Cr^{3+} concentration approaching the maximum at 0.4 at.% (see Fig. 8c,d). At higher chromium concentration the PL intensity decreases due to the concentration quenching as the distance between Cr^{3+} - Cr^{3+} ions decreases and energy transfer between the Cr^{3+} ions occurs (becomes more favourable). Based on Dexter's theory of energy transfer between luminescent species [45, 46], the critical distance between Cr^{3+} ions for energy transfer can be calculated using following equation (1):

$$
R_c \approx 2\left[\frac{3V}{4\pi x_c Z}\right]^{1/3} \tag{1}
$$

where *V* is the volume of the unit cell, x_c is the critical concentration of the doping ions and *Z* is the number of host cations in the unit cell. In case of α -Al₂O₃, *V* = 254.7 Å, *Z* = 12 and the critical concentration of Cr^{3+} ions in α -Al₂O₃ host is 0.004. The calculated critical distance R_c of Cr^{3+} ions is estimated to be 22 Å. The similar results were obtained for samples pre-sintered at 1390°C. The PL intensities in the spectra recorded using backscattering geometry (front-face

mode) are, however, somewhat higher than for the samples pre-sintered at 1380°C, that is a result of light scattering on samples with lower transparency. The maximum intensity of PL emission was found for concentration 0.4 at.% of Cr^{3+} in Al₂O₃ host matrix. The similar optimal Cr^{3+} concentration in Al₂O₃ host was reported for ruby crystal (0.15 mol.% Cr₂O₃) [28] and for powder Al₂O₃:Cr³⁺ phosphors in the range 0.1 at.% up to 1.0 at.% of Cr³⁺ [29, 33, 35, 36].

The crystal field parameters, crystal field strength *D*q, and Racah parameters *B* and *C* can be extracted from experimental excitation and emission spectra using transition energies between the ground state ${}^4A_{2g}({}^4F)$ and states ${}^4T_{2g}$, ${}^4T_{1g}({}^4F)$ and ${}^2E_g({}^2G)$ [20, 47]. The crystal field strength (D_q) can be roughly estimated by the peak energy of ⁴ A_{2g} ⁽⁴F) \rightarrow ⁴ T_{2g} ⁽⁴F) transition [20, 47]:

$$
D_q = \frac{E(^{4}A_{2g} \to {^{4}T_{2g}})}{10}
$$
 (2)

Based on the peak energy difference between ${}^4A_{2g}({}^4F) \rightarrow {}^4T_{1g}({}^4F)$ and ${}^4A_{2g}({}^4F) \rightarrow {}^4T_{2g}({}^4F)$ transitions, the value of the Racah parameter *B* can be calculated from the following expressions [20, 47]:

$$
\frac{D_q}{B} = \frac{15(x-8)}{(x^2 - 10x)}\tag{3}
$$

where the parameter *x* is defined as

$$
x = \frac{E(^{4}A_{2g} \rightarrow ^{4}T_{1g}) - E(^{4}A_{2g} \rightarrow ^{4}T_{2g})}{D_{q}}
$$
(4)

Finally, according to the peak energy of the emission ${}^2E_g({}^2G) \rightarrow {}^4A_{2g}({}^4F)$ transition, the Racah parameter *C* is evaluated by the equation (5) [20, 47]:

$$
E(^{4}A_{2g} \rightarrow {}^{2}E_{g}) = 3.05C + 7.08B - \frac{1.8B^{2}}{D_{q}}
$$
 (5)

In Tanabe-Sugano diagram for d³ electronic configuration, ${}^2E_g({}^2G)$ energy level is not sensitive to D_q while ⁴T_{2g}(⁴F) varies linearly with crystal field strength. The crossing of the ²E_g(²G) and ⁴T_{2g}(⁴F) levels occurs near D_q/B value \sim 2.3 (intermediate crystal field). According to common criterion, when $D_q/B > 2.3$ (strong crystal field), ²E_g level is lower than ⁴T_{2g} thus resulting in

sharp R-line emission. In weak crystal field $D_q/B < 2.3$, ⁴T_{2g} energy level is equal or lower than ${}^{2}E_{g}$ level thus broad emission band form ${}^{4}T_{2g}$ level to ground state can be observed. In the present work, the crystal field splitting parameter (D_0) for Cr^{3+} ion in α -Al₂O₃ host was found to be 1788 cm⁻¹. The calculated Racah *B* parameter is 676 cm⁻¹, and D_q/B value of 2.64 indicates that Cr^{3+} ions are positioned in the strong crystal field sites. The nephelauxetic ratio defined as $\beta = B/B_0$ ($B_0 = 918$ cm⁻¹ for free Cr³⁺ ion), which is a quantitative measure of the nephelauxetic effect is 0.74. This decrease in *B* value compared to the free ion value is due to partial covalency of Cr-O bond. The Racah parameter *C* is 3304 cm⁻¹ ($C_0 = 3850$ cm⁻¹ for free Cr³⁺ ion). The similar values of D_q and Racah parameters *B* and *C*, as those for the Cr^{3+} doped transparent alumina ceramics in the present study were found for ruby single crystals and $Al_2O_3:Cr^{3+}$ powder phosphors [20, 30, 39].

The competition between the covalence and the ionicity of the chemical bond is the key-factor that determines values of the *B* and *C* parameters. In more covalent hosts, such as oxides, when covalent interaction between the 3d ions and ligand anions is enhanced the *B* and *C* parameters are significantly reduced. The nephelauxetic parameter β , however, completely ignores the role of the parameter *C*, which is rather crude approximation. Brik et al. [20] suggested to modify this parameter and included also the Racah parameter *C*; $\beta_1 = \sqrt{(B/B_0)^2 + (C/C_0)^2}$. The parameter β_1 was used to predict the energy of the ²E_g(²G) \rightarrow ⁴A_{2g}(⁴F) transition by applying an empirical linear relation, i.e. $E(^{2}E_{g} \rightarrow {}^{4}A_{2g}) = 3382.80 + 10021.47 \beta_{1}$ with the rms deviation of 362 cm⁻¹, based on the large number of experimental data of Cr^{3+} -doped oxide materials. For Al₂O₃:Cr³⁺ studied samples, β_1 is 1.13, the ²E_g energy position is then calculated as \sim 14700 $cm⁻¹$, the value that is not so far form the experimental value 14412 $cm⁻¹$.

To study the luminescence dynamics, luminescence decay curves of Al_2O_3 : Cr^{3+} transparent polycrystalline ceramics pre-sintered at 1380°C with different dopant concentrations were recorded under excitation with pulsed Xe-lamp (see Fig. 9) at room temperature. The samples were excited at 404 nm and emissions were monitored at 694 nm. The PL decay curves can be well fitted with single exponential decay function:

$$
I_{t} = I_{0} \exp(-t/\tau), \tag{6}
$$

where I_t is the intensity at time t , I_0 is the intensity at $t = 0$, and τ is decay lifetime. The fitted fluorescence lifetime values for Al_2O_3 : Cr^{3+} transparent ceramics samples are about 3.60 ± 0.01 ms and are not significantly affected by the Cr³⁺ concentration in the host matrix within the concentration range up to 0.4 at. % of Cr^{3+} . Then, the decay time stars to decrease slightly due to the concentration quenching as also documented by PL intensity decrease at concentrations higher than 0.4 at. % of Cr^{3+} in the Al₂O₃ host; for sample containing 0.75 at. % of $Cr^{3+} \tau$ value was found to be 3.52 \pm 0.01 ms. The values are similar to the value reported in literature of about 3 ms at 300 K for ruby single crystal [42]. The lifetime values for samples pre-sintered at 1390°C were almost identical to lifetime values of samples pre-sintered at 1380°C for particular dopant concentration, so pre-sintering regime had no effect on luminescence dynamics in prepared samples.

4. Conclusions

Transparent polycrystalline chromium doped alumina with photoluminescent properties were prepared and characterised in this study. The preparation method consisting of slip casting of fine alumina suspension doped with nano- Cr_2O_3 followed by pre-sintering under ambient conditions and hot isostatic pressing at 200 MPa of argon was found to be successful in preparation of transparent Cr^{3+} doped alumina. The optical transmittance and the real in-line transmittance are strongly related to the grain size: proper adjustment of sintering conditions limiting the grain growth is crucial for achieving the transparency. Even mild grain size increase results in the significant transparency decrease. The effect of chromium concentration on the transmittance and RIT in examined range is less pronounced, and only a slight influence was observed in the wavelength region where the light is absorbed by Cr^{3+} dopant ions. The UV-VIS-NIR transmission spectra exhibit two broad bands with the maxima at 403 nm and 558 nm and one "line" band of low intensity at 694 nm corresponding to absorption of Cr^{3+} ions. The absorbance increases with increasing Cr^{3+} concentration in the samples and calculated molar absorption coefficients (using the linear fit) for violet and green absorption were found to be 3.8×10^4 mol⁻¹cm² (38 L⁻¹mol⁻¹cm) and 2.4×10^4 mol⁻¹cm² (24 L⁻¹mol⁻¹cm), respectively. Almost identical values were found for samples pre-sintered at 1390° C (36 and 24 L⁻¹mol⁻¹cm). Absorption cross-section values, σ , for violet and green absorption were calculated to be 1.45×10^{-19} cm² and 9.22×10^{-20} cm², respectively. These data are in a good agreement with values reported either for ruby single crystals or for polycrystalline Cr^{3+} -doped alumina. The excitation spectra consist of two broad bands with maxima at 404 nm and 558 nm, corresponding to ${}^4A_{2g} \rightarrow {}^4T_{1g}$ and ${}^4A_{2g} \rightarrow {}^4T_{2g}$ transitions of Cr³⁺ ions in octahedral sites of α -Al₂O₃, and with intensity ratio dependent on the Cr^{3+} concentration. The intensive deep red narrow emissions under violet/green light excitation, R-lines $(^{2}E_{g} \rightarrow {}^{4}A_{2g}$ transition), were observed at 692.5 and 693.8 nm, that are very close to ruby single crystal. The optimal Cr^{3+}

doping concentration was found to be 0.4 at.%, with the critical distance between Cr^{3+} ions for energy transfer (concentration quenching), based on Dexter's theory, of 22 Å. The D_q/B parameter value of 2.64 indicates that Cr^{3+} ions are positioned in the strong crystal field sites. The calculated Racah parameter B was found to be 676 cm^{-1} and parameter C is 3304 cm⁻¹. The reduction in the values of Racah parameters compared to the values of free Cr^{3+} ions is due to partial covalency of Cr-O bond. The luminescence decay curves exhibit single-exponential behaviour with decay times of \sim 3.6 ms, similar to ruby monocrystal, and decay is only slightly affected by the Cr^{3+} concentration.

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Figure captions

Fig. 1 Dependence of relative density of pre-sintered samples on the temperature.

Fig. 2 The photo of HIP-ed samples. The samples are placed 5 mm above the surface.

Fig. 3 Dependence of mean grain size on Cr^{3+} content in alumina ceramics after HIP.

Fig. 4 Positive mode TOF-SIMS mass spectrum in the mass range from m/z 20 to m/z 100

with detail in the mass range from m/z 49 to m/z 55 of the sample containing 0.5 at.% of

 Cr^{3+} pre-sintered at 1380°C after HIP; and TOF-SIMS images of Al⁺ and Cr^+ distribution.

Fig. 5 Dependence of RIT on the Cr^{3+} content in alumina ceramics.

Fig. 6 Transmission spectra of polycrystalline Cr^{3+} -doped alumina transparent ceramic samples prepared using pre-sintering regime 1380°C/2min and HIP 1200°C/3h (a). Inset represents enlarged area of the Cr^{3+} absorptions in spectral range from 200 nm to 800 nm. All data are recalculated to sample thickness of 0.8 mm for comparison. (b) Absorption spectra of polycrystalline doped transparent alumina.

Fig. 7 Excitation spectra of Cr^{3+} -doped alumina transparent ceramic samples prepared using pre-sintering regime 1380° C/2min and HIP 1200° C/3h, $\lambda_{\text{mon}} = 694$ nm.

Fig. 8 Emission spectra of the Al_2O_3 : Cr^{3+} transparent ceramics prepared using pre-sintering regime 1380°C/2min and HIP 1200°C/3h: (a) sample containing 0.1 at.% of Cr^{3+} under excitation by violet (404 nm) and green (560 nm) light; (b, c) emission spectra Al_2O_3 ceramics with different concentration of Cr^{3+} (0.1 – 0.5 at.%) in host matrix under excitation at 404 nm. Inset represents enlarged area of low intensity N-lines and sidebands in the spectral range from 650 nm to 740 nm. (d) PL integrated intensity as a function of Cr^{3+} concentration.

Fig. 9 The decay curves of the Al_2O_3 : Cr^{3+} transparent ceramics with different concentration of Cr^{3+} (0.1 – 0.5 at.%).

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Figure 1

